

Mixed LoS/NLoS Near-Field Channel Estimation for Extremely Large-Scale MIMO Systems

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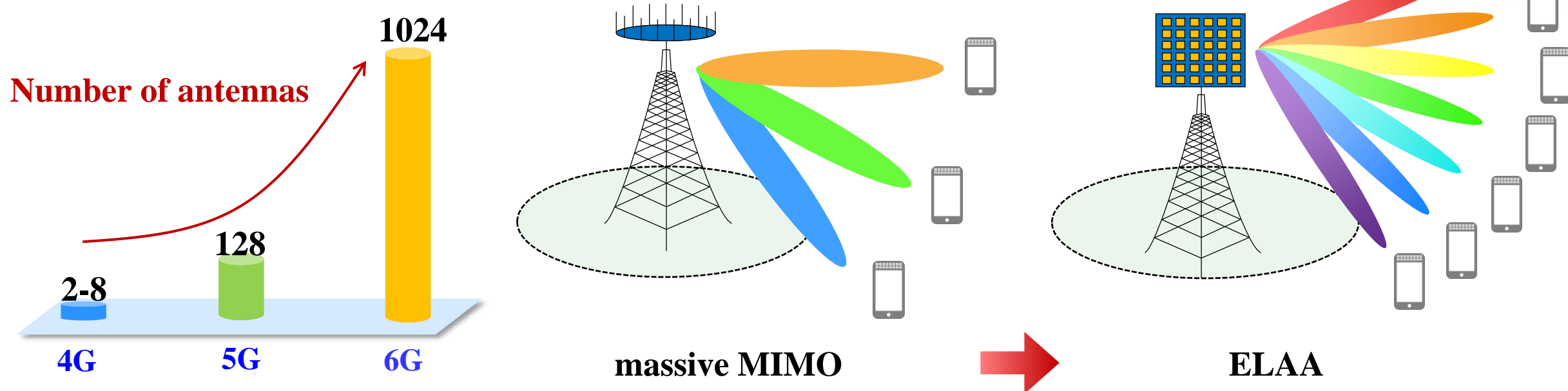
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Extremely Large-Scale Antenna Array



- 6G is expected to achieve **10 times higher spectral efficiency** compared with 5G
- The higher spectral efficiency can be achieved by exploiting **spatial multiplexing**, which requires significantly increased number of antennas
 - 4G: 2-8 antennas → 5G: 64-256 antennas
 - 6G: 1024+ antennas with **extremely large-scale antenna array (ELAA)**



[1] W. Jiang, B. Han, M. A. Habibi and H. D. Schotten, "The Road Towards 6G: A Comprehensive Survey," *IEEE Open J. Commun. Soc.*, vol. 2, pp. 334-366, Feb. 2021.

Near-Field for ELAA



- Electromagnetic propagation can be divided into **far-field** and radiative **near-field** region

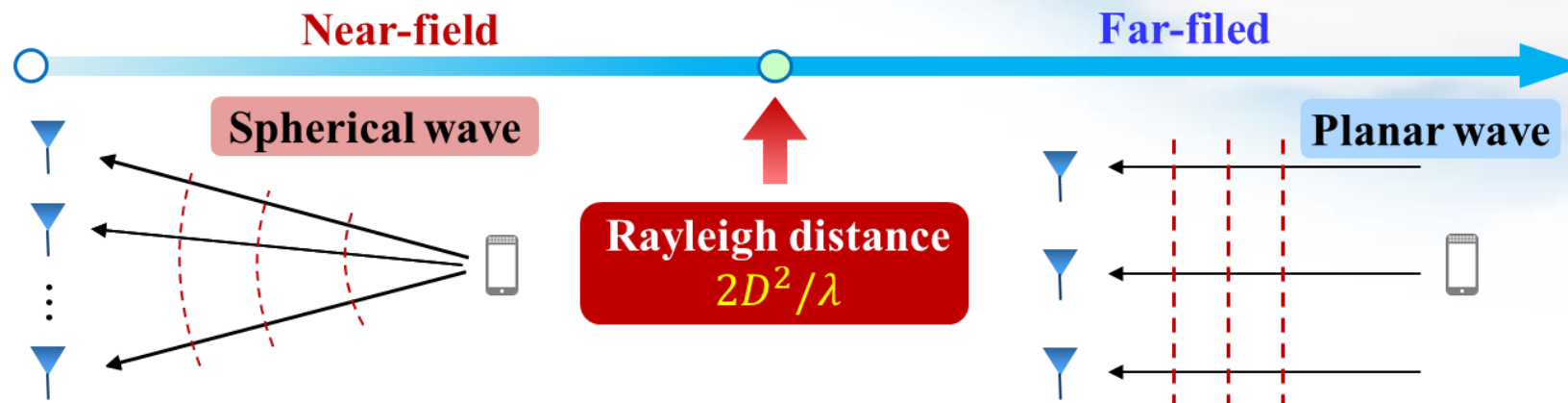
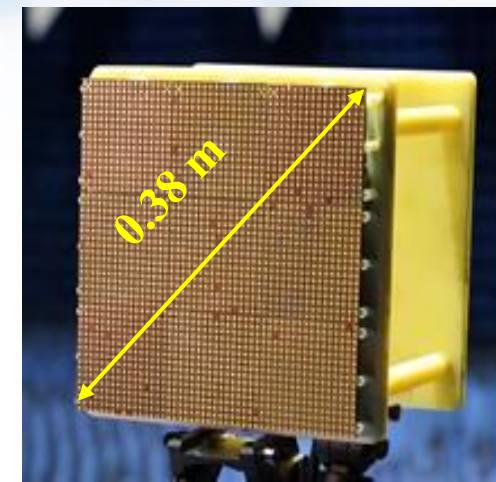


Table I. **Near-field region** [m] (data from [1])

	0.1 m	0.5 m	1 m	3 m
3 GHz	0.21	5	20	180
28 GHz	1.9	47	187	/
142 GHz	9.0	237	/	/



ELAA with 2304 antennas @ 28GHz, Rayleigh distance is 25 m, Tsinghua [2]

Evolution from massive MIMO to extremely large-scale array results in the near-field propagation

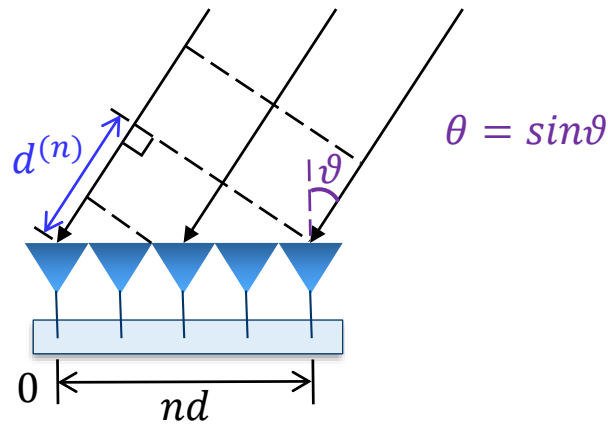
[1] A. Pizzo, L. Sanguinetti, and T. L. Marzetta, "Fourier plane-wave series expansion for holographic MIMO communications," *IEEE Trans. Wireless Commun.*, vol. 21, no. 9, pp. 6890-6905, Sep. 2022.

[2] M. Cui, Z. Wu, Y. Chen, S. Xu, F. Yang, and L. Dai, "Demo: Low-power communications based on RIS and AI for 6G," in *Proc. IEEE Int. Conf. Commun. (IEEE ICC'22)*, Seoul, SouthKorea, May 2022. (**IEEE ICC 2022 Outstanding Demo Award**).

Far-Field vs. Near-Field

- **Far-field:** the EM waves impinging on the antenna array can be approximately modeled as **planar waves**, where the phase of the EM wave is a **linear function** of the antenna index
- **Near-field:** the EM waves have to be accurately modeled as **spherical waves**, where the phase of the EM wave is a **non-linear function** of the antenna index

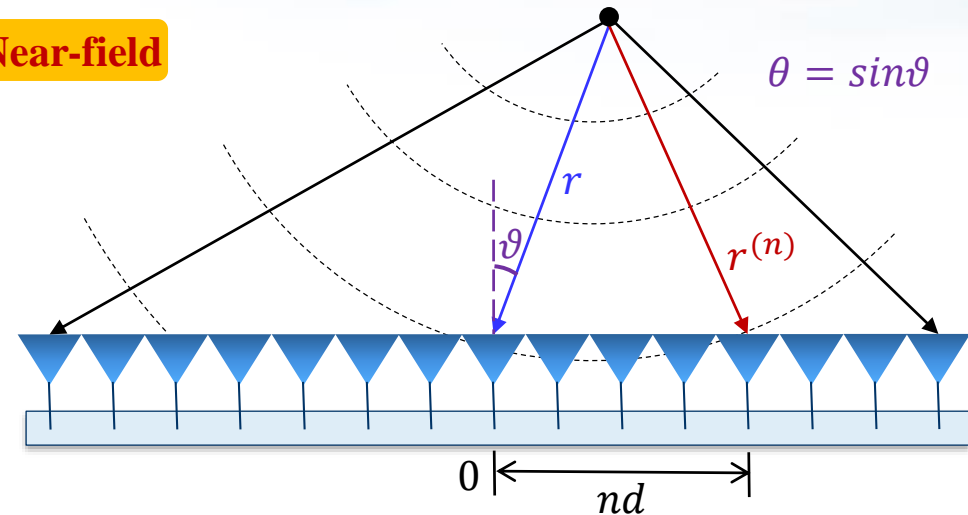
Far-field



Distance: $d^{(n)} = nd\theta$ **Linear**

Phase: $\phi_n^{\text{far}} = -\frac{2\pi d^{(n)}}{\lambda} = -\frac{2\pi}{\lambda} nd\theta$

Near-field



Distance: $r^{(n)} = \sqrt{r^2 + n^2 d^2 - 2n d r \theta}$ **Non-linear**

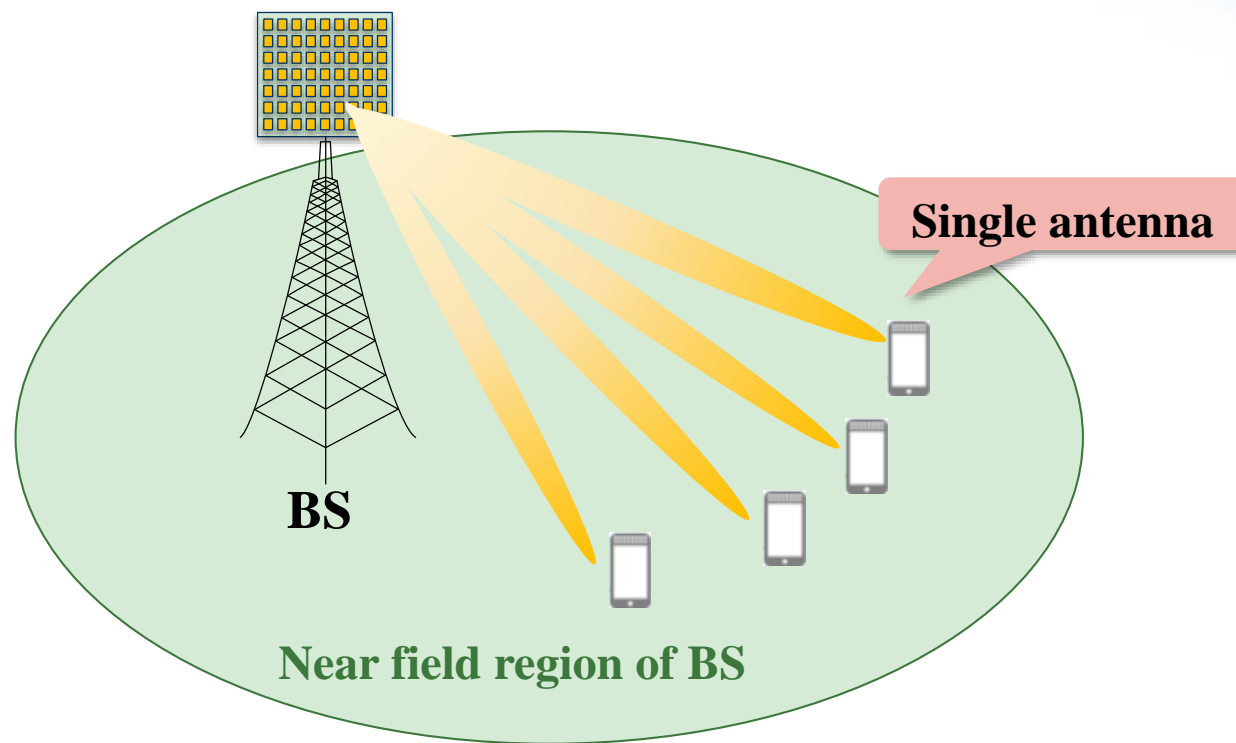
Phase: $\phi_n = \frac{2\pi(r^{(n)} - r)}{\lambda} = \frac{2\pi}{\lambda} (\sqrt{r^2 + n^2 d^2 - 2n d r \theta} - r)$

Antenna index: $n \in [-N, \dots, 0, \dots, N]$ Antenna number: $M = 2N + 1$

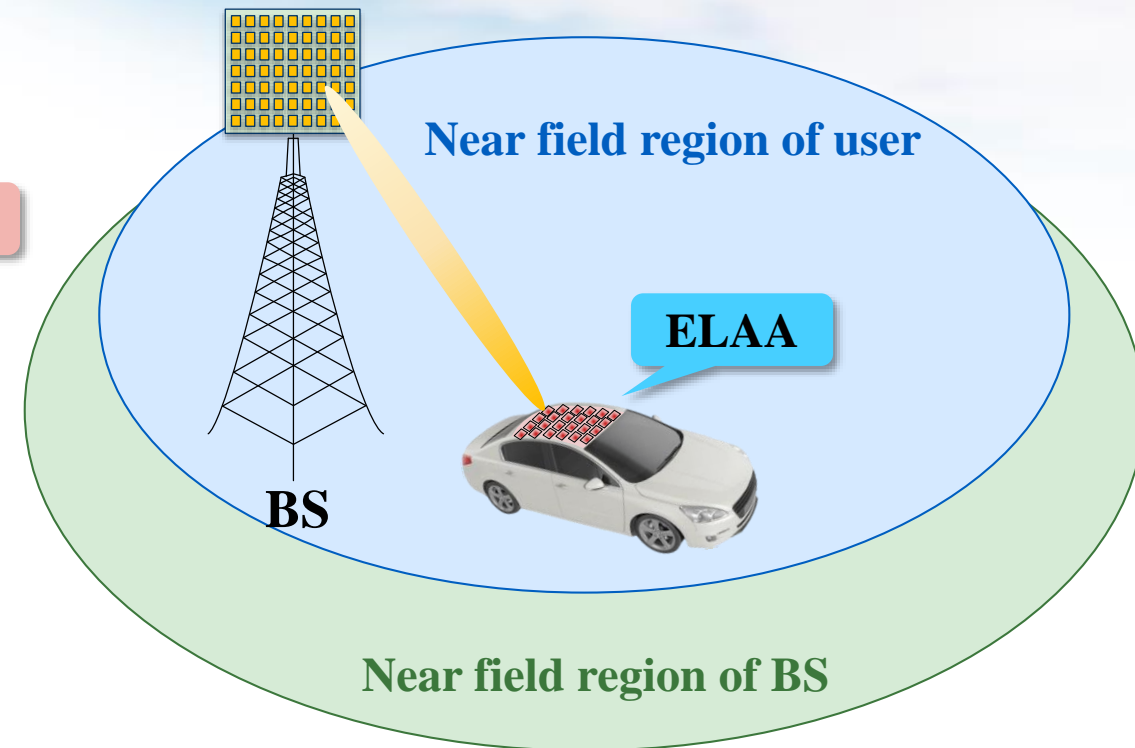
Near-Field: From MISO to MIMO



- **MISO**: Only the BS is equipped with **extremely large-scale antenna array (ELAA)**
- **MIMO**: Both the BS and the user are equipped with **ELAA**



MISO



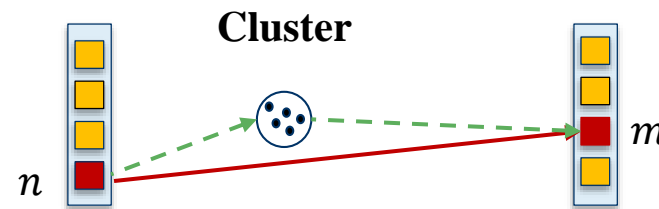
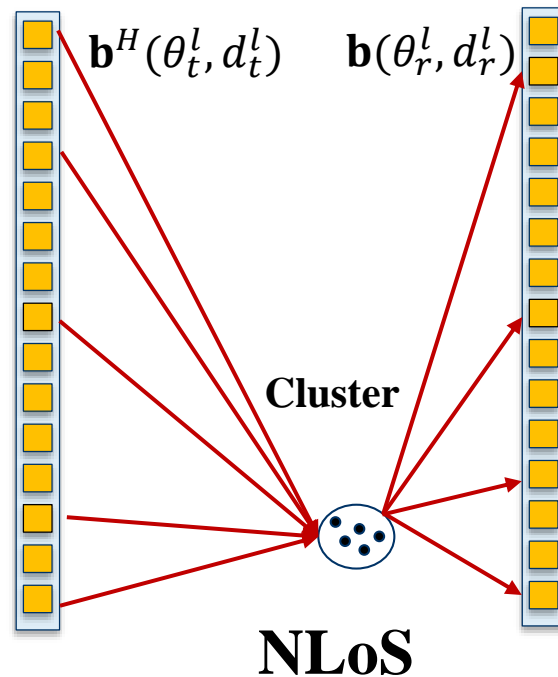
MIMO

Near-Field MIMO Channel Model

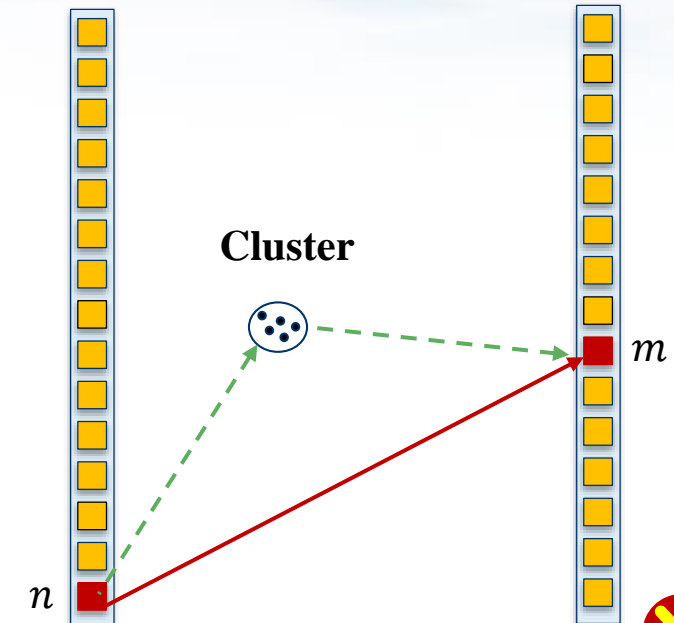


- Similar to far-field MIMO channel model, the existing near-field MIMO channel model is based on the near-field array response vector

$$\mathbf{H}_{\text{near-field}} = \sqrt{\frac{N_1 N_2}{L}} \sum_{l=1}^L g_l \mathbf{b}(\theta_r^l, d_r^l) \mathbf{b}^H(\theta_t^l, d_t^l)$$



Far-field LoS



Near-field LoS

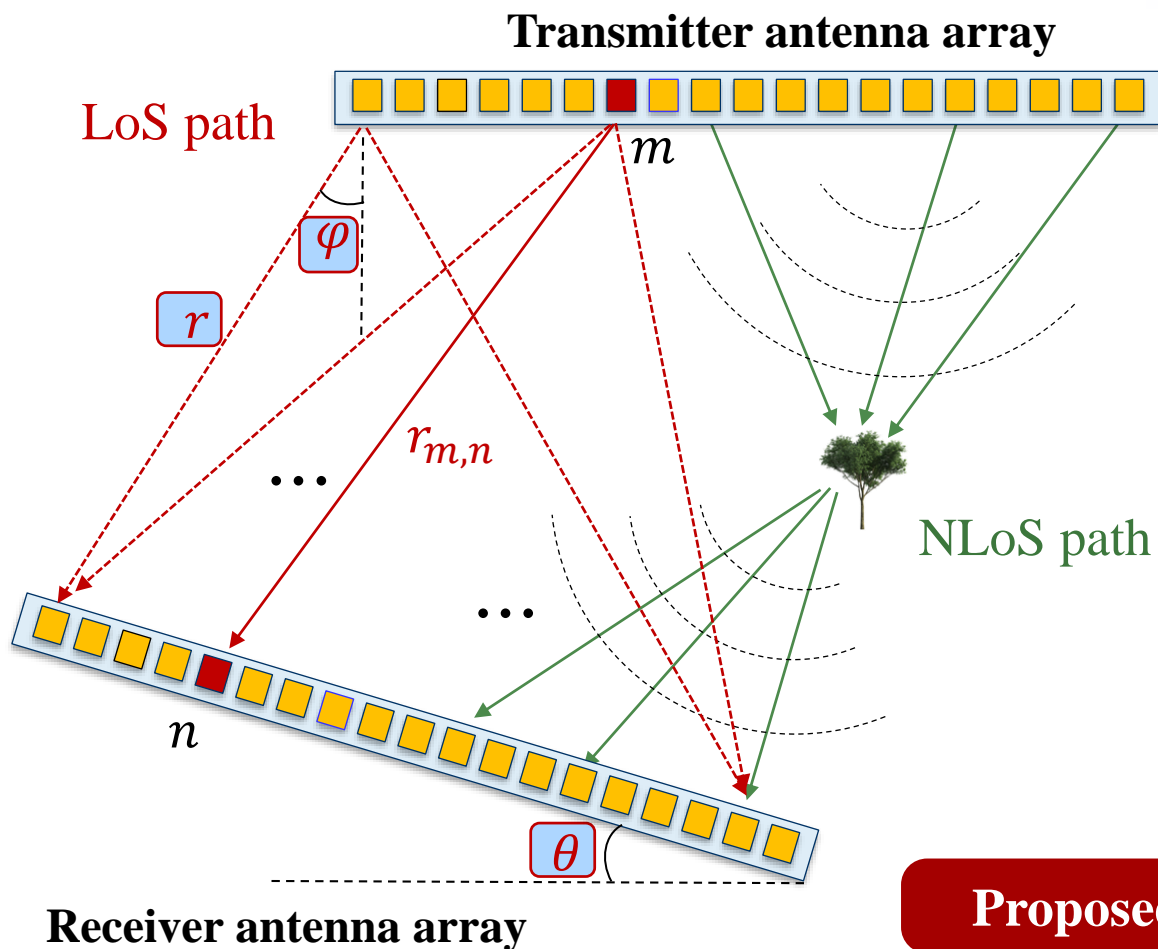


The existing model cannot accurately describe the characteristic of **near-field LoS path**

Near-Field MIMO Channel Model



- The LoS and NLoS paths are modeled separately



LoS: Free space propagation assumption

$$\mathbf{H}_{\text{LoS},(m,n)} = \frac{e^{-j2\pi r_{m,n}/\lambda}}{r_{m,n}}$$

$$r_{m,n} = \sqrt{r^2 + (md)^2 + (nd)^2 - 2rmd\cos(\theta + \varphi) + 2rnd\cos(\theta) - 2mnr^2\cos(\varphi)}$$

$$\mathbf{H}_{\text{LoS}}(r, \theta, \varphi) = \begin{bmatrix} \frac{e^{-j2\pi r_{1,1}/\lambda}}{r_{1,1}} & \cdots & \frac{e^{-j2\pi r_{1,N}/\lambda}}{r_{1,N}} \\ \vdots & \ddots & \vdots \\ \frac{e^{-j2\pi r_{M,1}/\lambda}}{r_{M,1}} & \cdots & \frac{e^{-j2\pi r_{M,N}/\lambda}}{r_{M,N}} \end{bmatrix}$$

NLoS: Based on array steering vector

$$\mathbf{H}_{\text{NLoS}} = \sum_{l=1}^L g_l \mathbf{a}(\theta_r^l, r_r^l) \mathbf{b}^H(\theta_t^l, r_t^l)$$

Proposed near-field MIMO channel model: $\mathbf{H} = \mathbf{H}_{\text{LoS}} + \mathbf{H}_{\text{NLoS}}$

Near-Field MIMO Rayleigh Distance



- **Rayleigh Distance:** The transceiver distance when the maximum difference between spherical wave and plane wave is $(\pi/8)$

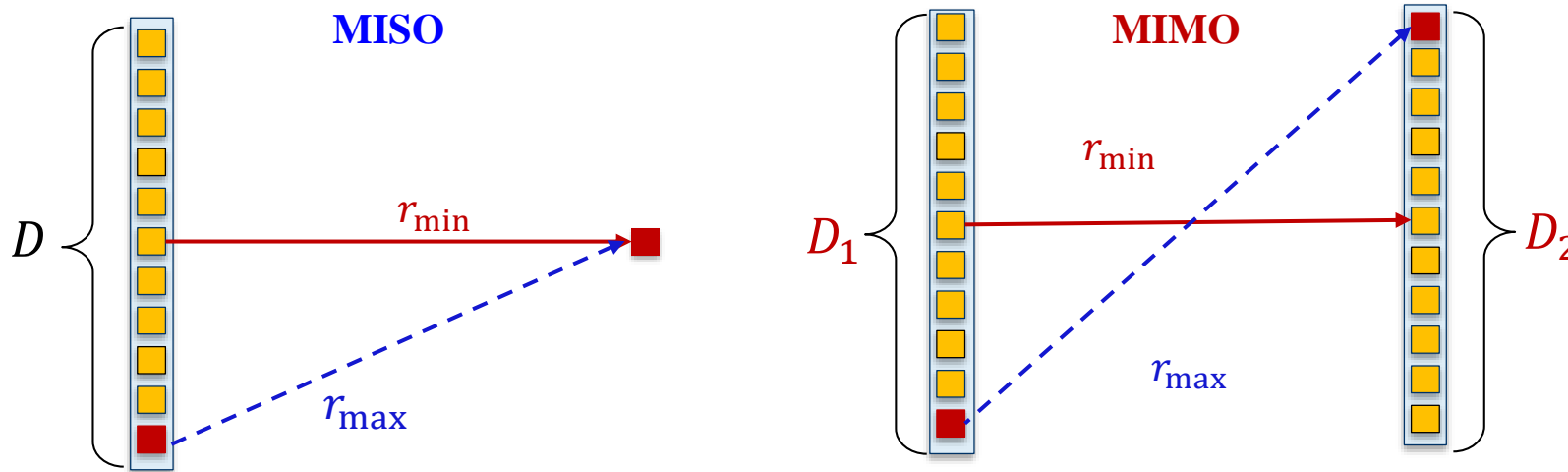
Array aperture

➤ **Classical MISO** Rayleigh Distance: $R_1 = 2D^2/\lambda$

Sum of transmitter and receiver array apertures

➤ **Proposed MIMO** Rayleigh Distance :

$$R_2 = 2(D_1 + D_2)^2/\lambda$$



MIMO-RD is larger than MISO-RD

Near-Field MIMO Channel Estimation



- The proposed channel estimation scheme based on near-field MIMO channel model

Received pilot

Transmitted pilot

Noise

$$\mathbf{Y}_{N_2 \times M} = \mathbf{H}_{N_2 \times N_1} \mathbf{P}_{N_1 \times M} + \mathbf{N}_{N_2 \times M}$$

$$\mathbf{H}_{LOS} + \mathbf{H}_{NLOS}$$

Maximum likelihood

Utilize polar-domain sparsity

$$\min_{r, \theta, \varphi} \|\mathbf{Y} - \mathbf{H}_{LOS}(r, \theta, \varphi) \mathbf{P}\|^2$$

$$\text{s. t. } (r, \theta, \varphi) \in \Xi$$

$$\Xi = \{(r, \theta, \varphi) |$$

$$1/r = 1/r_{max}, 1/r_{max} + 1/\Delta r, \dots, 1/r_{min};$$

$$\theta = \theta_{min}, \theta_{min} + \Delta\theta, \dots, \theta_{max};$$

$$\varphi = \varphi_{min}, \varphi_{min} + \Delta\varphi, \dots, \varphi_{max}\}$$

Remove $\hat{\mathbf{H}}_{LoS}$ component:

$$\mathbf{Y}_{NLoS} = \mathbf{Y} - \hat{\mathbf{H}}_{LoS} \mathbf{P}$$

Estimate \mathbf{H}_{NLoS} with \mathbf{Y}_{NLoS} and \mathbf{P} :

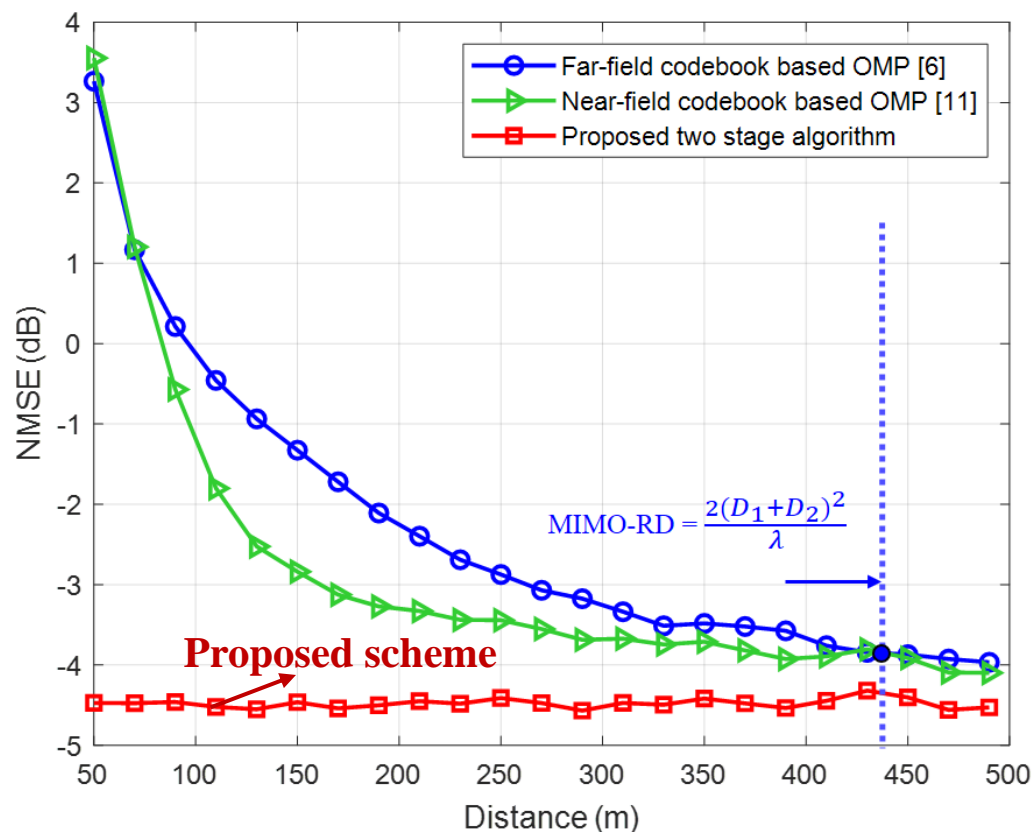
$$\mathbf{Y}_{NLoS} = \mathbf{H}_{NLoS} \mathbf{P} + \mathbf{N}$$

Vectorize the equation and formulate as **sparse signal reconstruction problem** with **sparse channel \mathbf{h}_{NLoS}^P**

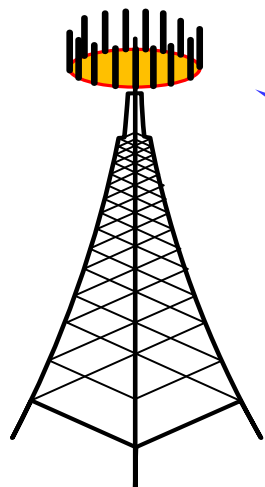
$$\mathbf{y}_{NLoS} = \mathbf{A} \mathbf{h}_{NLoS}^P + \mathbf{n}$$

Simulation Results

- The proposed schemes can accurately estimate the near-field MIMO channel.



Parameters	Value
Carrier	10 GHz
Element number of transmitter antenna array	128
Element number of receiver antenna array	64
Number of NLoS Paths	5
SNR	5 dB
Pilot compression ratio	0.5



Thanks



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